**NC STATE UNIVERSITY** 



# Quantifying uncertainties in watershed nutrient loads: apportionment of uncertainty sources

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#### Monitoring water quality in agricultural watersheds





# Sources of uncertainties when measuring nutrient loads

- Uncertainties on flow rates and cumulated flow
- Uncertainties associated with infrequent sampling
- Uncertainties due to the sampling location in the water column
- Uncertainties due to sample degradation between sampling and analysis
- Uncertainties of laboratory analyses



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#### **Optimizing Monitoring**



• What should I be particularly careful about to lower uncertainties on loads and improve confidence in my results?



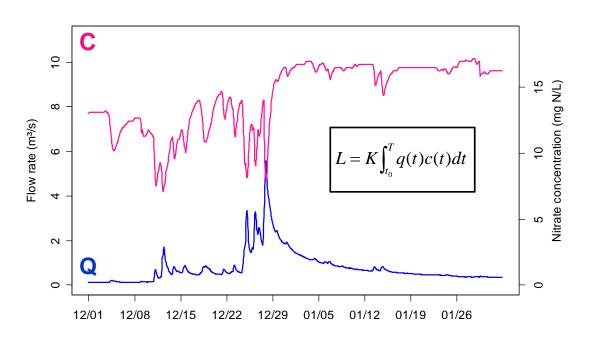
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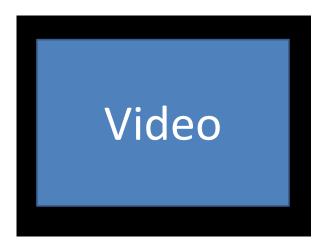
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#### In a perfect world, perfect continuous data...





# Video: daily sampling interval





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## Sampling interval: 6 days





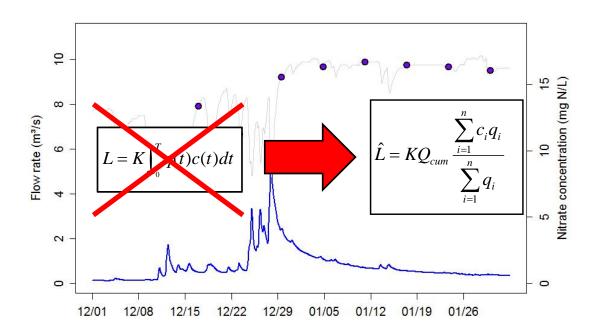
# Sampling interval: 10 days



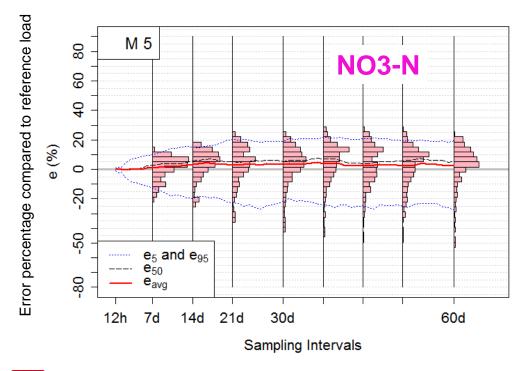


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#### Flow weighted average: least bad method





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#### Uncertainties on flow

- Difficult to fully estimate
- Approach chosen:
  - Flow estimated using rating curves
  - Errors due to
    - o number of gauged points,
    - o hysteresis of the stage discharge relationship
    - Mathematical relationship chosen as rating curve



# Video: 10 gauging points

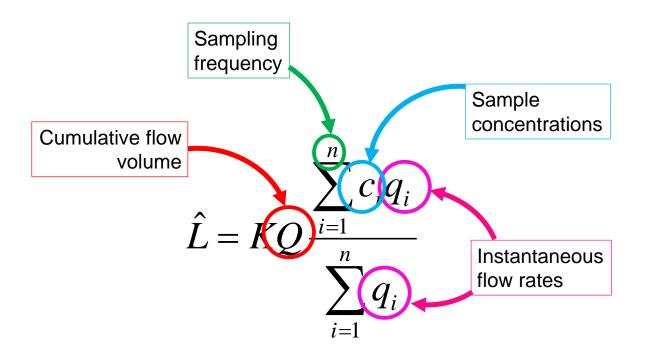




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Video: 26 gauging points

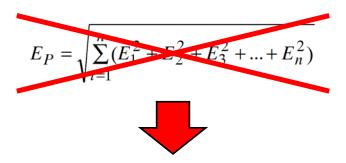
Video





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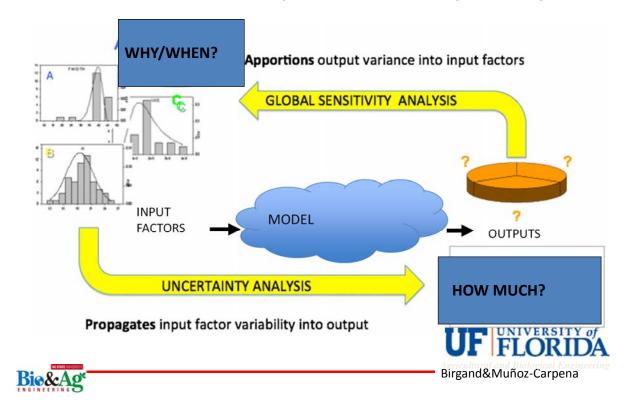
### Calculating cumulative uncertainty



Global Sensitivity Analysis (GSA)

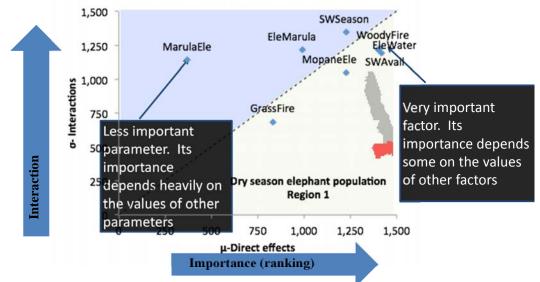


#### Global Sensitivity/Uncertainty Analysis



# Step 1: Screening (Morris Method)

• qualitative measure of importance ( $\mu^*$ ) and interaction ( $\sigma$ ) of input factors



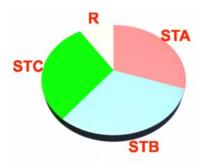
Used as a screening method to reduce number of important factors



#### **Step 2: Variance Decomposition**

$$V(Y) = V_1 + V_2 + ... + V_k + R$$

V(Y) – variance of output, V<sub>i</sub> – variance due input factor X<sub>i</sub>, k - nr of uncertain factors, R - residual

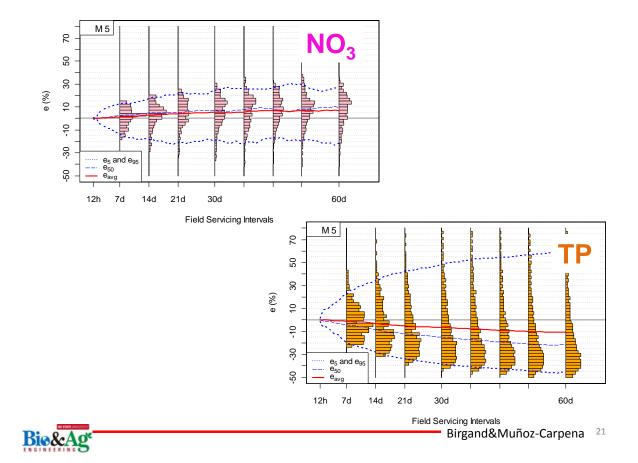




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#### **Simulations**

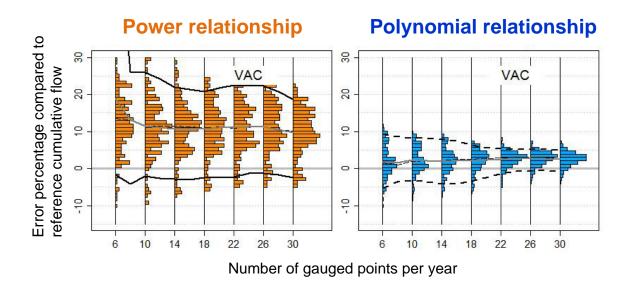
- Reference data with continuous Q and WQ
- Errors on annual loads
- Variables
  - o NO<sub>3</sub>, TP
  - Sampling frequency



#### **Simulations**

- Reference data with continuous Q and WQ
- Errors on annual loads
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  - Number of gauged points
  - Type of rating curve





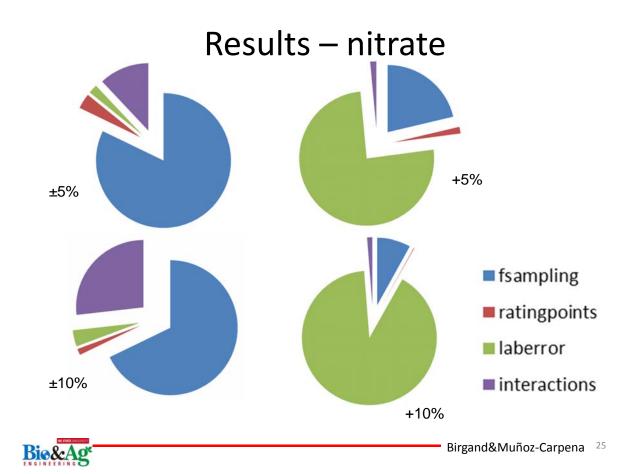


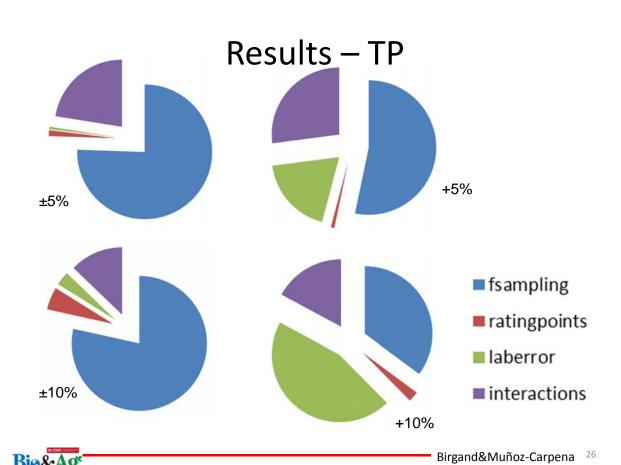
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# **Simulations**

- Reference data with continuous Q and WQ
- Errors on annual loads
- Variables
  - o NO<sub>3</sub>, TP
  - Sampling frequency
  - Number of gauged points
  - Type of rating curve
  - o Lab errors: systematic (e.g. + 5%) or random (e.g. ±5%)







#### Conclusion

- The GSA approach very useful tool for uncertainties on nutrient loads
- Random lab errors weigh little on the overall uncertainties
- Errors due to the number of gauged points small
- Rating curve type very important
- Results may vary dramatically with watersheds and nutrients



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